

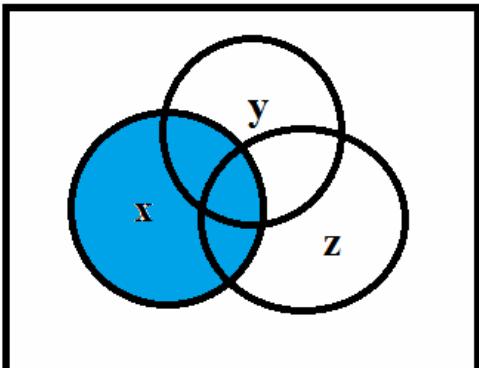
Solution of Homework-1

2.2 Use the algebraic manipulation to prove that $(x + y).(x + \bar{y}) = x$

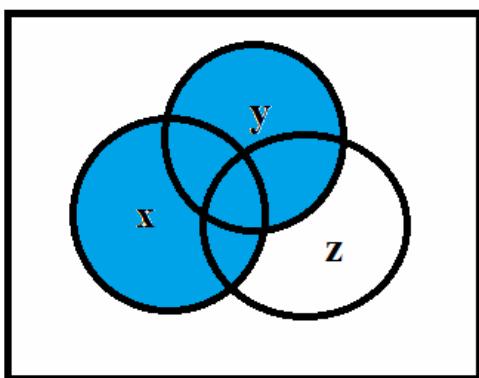
Solution:

$$\begin{aligned} LHS &= (x + y).(x + \bar{y}) \\ &= x.x + x.y + x.\bar{y} + y.\bar{y} \\ &= x(x + y + \bar{y}) + 0 \\ &= x(x + 1) = x.1 = x \end{aligned}$$

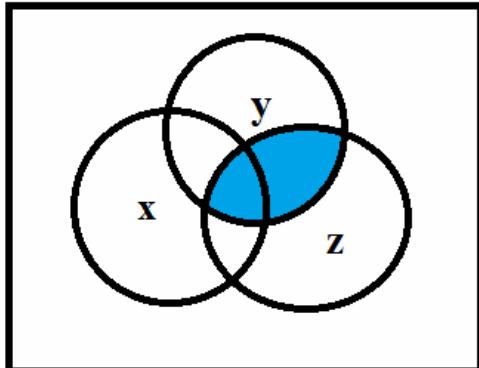
2.4 Use the Venn diagram to prove the identity $x + yz = (x + y)(x + z)$



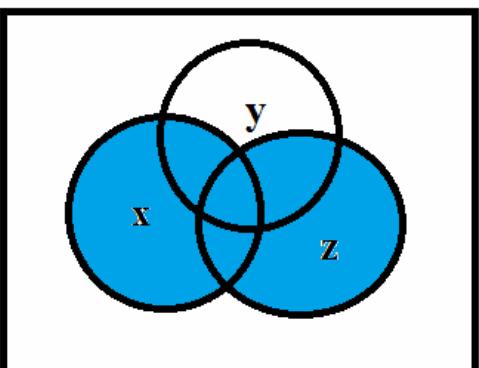
x



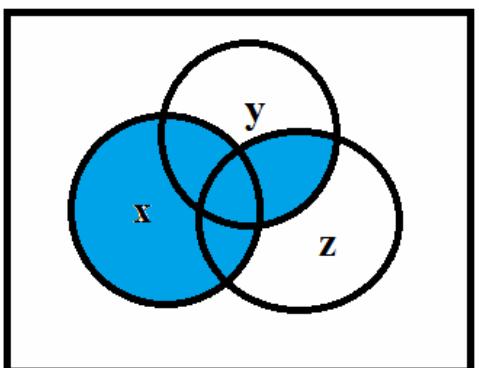
$x+y$



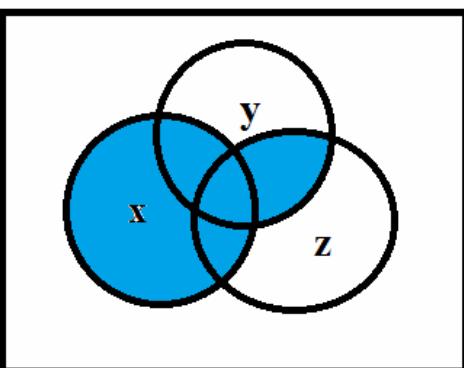
$y.z$



$x+z$



$x+y.z$



$(x+y)(x+z)$

2.7 Determine whether or not the following expressions are valid, i.e., whether the left and the right hand sides express the same function.

$$(a) \overline{x_1}x_3 + x_1\overline{x_2}x_3 + \overline{x_1}\overline{x_2} + x_1\overline{x_2} = \overline{x_2}x_3 + x_1\overline{x_3} + x_2\overline{x_3} + \overline{x_1}\overline{x_2}x_3$$

$$(b) x_1\overline{x_3} + x_2\overline{x_3} + \overline{x_2}x_3 = (x_1 + \overline{x_2} + x_3)(x_1 + x_2 + \overline{x_3})(\overline{x_1} + x_2 + \overline{x_3})$$

$$(c) (x_1 + x_3)(\overline{x_1} + \overline{x_2} + \overline{x_3})(\overline{x_1} + x_2) = (x_1 + x_2)(x_2 + x_3)(\overline{x_1} + \overline{x_3})$$

Solution:

(a) Using the truth table

LHS

x_1	x_2	x_3	\bar{x}_1x_3	$x_1\bar{x}_2\bar{x}_3$	\bar{x}_1x_2	$x_1\bar{x}_2$	$\bar{x}_1x_3 + x_1\bar{x}_2\bar{x}_3 + \bar{x}_1x_2 + x_1\bar{x}_2$
0	0	0	0	0	0	0	0
0	0	1	1	0	0	0	1
0	1	0	0	0	1	0	1
0	1	1	1	0	1	0	1
1	0	0	0	0	0	1	1
1	0	1	0	0	0	1	1
1	1	0	0	1	0	0	1
1	1	1	0	0	0	0	0

RHS

x_1	x_2	x_3	\bar{x}_2x_3	$x_1\bar{x}_3$	$x_2\bar{x}_3$	$\bar{x}_1x_2x_3$	$\bar{x}_2x_3 + x_1\bar{x}_3 + x_2\bar{x}_3 + \bar{x}_1x_2x_3$
0	0	0	0	0	0	0	0
0	0	1	1	0	0	0	1
0	1	0	0	0	1	0	1
0	1	1	0	0	0	1	1
1	0	0	0	1	0	0	1
1	0	1	1	0	0	0	1
1	1	0	0	1	1	0	1
1	1	1	0	0	0	0	0

Valid.

(b) Using the truth table

LHS

x_1	x_2	x_3	$x_1\bar{x}_3$	x_2x_3	$\bar{x}_2\bar{x}_3$	$x_1\bar{x}_3 + x_2x_3 + \bar{x}_2\bar{x}_3$
0	0	0	0	0	1	1
0	0	1	0	0	0	0
0	1	0	0	0	0	0
0	1	1	0	1	0	1
1	0	0	1	0	1	1
1	0	1	0	0	0	0
1	1	0	1	0	0	1
1	1	1	0	1	0	1

RHS

x_1	x_2	x_3	$(x_1 + \bar{x}_2 + x_3)$	$(x_1 + x_2 + \bar{x}_3)$	$(\bar{x}_1 + x_2 + \bar{x}_3)$	$(x_1 + \bar{x}_2 + x_3)(x_1 + x_2 + \bar{x}_3)(\bar{x}_1 + x_2 + \bar{x}_3)$
0	0	0	1	1	1	1
0	0	1	1	0	1	0
0	1	0	0	1	1	0
0	1	1	1	1	1	1
1	0	0	1	1	1	1
1	0	1	1	1	0	0
1	1	0	1	1	1	1
1	1	1	1	1	1	1

Valid.

(c) Using the truth table

LHS

x_1	x_2	x_3	$(x_1 + x_3)$	$(\bar{x}_1 + \bar{x}_2 + \bar{x}_3)$	$(\bar{x}_1 + x_2)$	$(x_1 + x_3)(\bar{x}_1 + \bar{x}_2 + \bar{x}_3)(\bar{x}_1 + x_2)$
0	0	0	0	1	1	0
0	0	1	1	1	1	1
0	1	0	0	1	1	0
0	1	1	1	1	1	1
1	0	0	1	1	0	0
1	0	1	1	1	0	0
1	1	0	1	1	1	1
1	1	1	1	0	1	0

RHS

x_1	x_2	x_3	$(x_1 + x_2)$	$(x_2 + x_3)$	$(\bar{x}_1 + \bar{x}_3)$	$(x_1 + x_2)(x_2 + x_3)(\bar{x}_1 + \bar{x}_3)$
0	0	0	0	0	1	0
0	0	1	0	1	1	0
0	1	0	1	1	1	1
0	1	1	1	1	1	1
1	0	0	1	0	1	0
1	0	1	1	0	0	0
1	1	0	1	1	1	1
1	1	1	1	0	0	0

Not valid.